

Chem 151. R. Corn

Diprotic Weak Acid

Constants:  $K_{a1}$ ,  $K_{a2}$ ,  $K_w$ ,  $C_0$

Five species:  $[H_2A]$ ,  $[HA^-]$ ,  $[A^{2-}]$ ,  $[H^+]$ ,  $[OH^-]$

$$K_{a1} = \frac{[H^+][HA^-]}{[H_2A]} \quad \text{acid dissociation 1}$$

$$K_{a2} = \frac{[H^+][A^{2-}]}{[HA^-]} \quad \text{acid dissociation 2}$$

$$K_w = [H^+][OH^-] \quad \text{water dissociation}$$

$$[H^+] = [HA^-] + 2[A^{2-}] + [OH^-] \quad \text{charge balance}$$

$$C_0 = [H_2A] + [HA^-] + [A^{2-}] \quad \text{mass balance}$$

Alpha Fractions

$$[H_2A]/C_0 = (1 + K_{a1}/[H^+] + K_{a1}K_{a2}/[H^+]^2)^{-1}$$

$$[HA^-]/C_0 = ([H^+]/K_{a1} + 1 + K_{a2}/[H^+])^{-1}$$

$$[A^{2-}]/C_0 = ([H^+]/K_{a2} + [H^+]^2/K_{a1}K_{a2} + 1)^{-1}$$

Iterative eqns for  $[H^+]$

$$[H^+][HA^-] = K_{a1}[H_2A]$$

$$[H^+]([H^+] - [OH^-] - 2[A^{2-}]) = K_{a1}[H_2A]$$

$$[H^+]^2 - 2[H^+][A^{2-}] - K_w = K_{a1}[H_2A]$$

$$[H^+]^2 = K_{a1}[H_2A] + 2K_{a2}[HA^-] + K_w$$

$$\text{Initial Guess: } [H^+] = \sqrt{K_{a1}C_0 + K_w}$$

Calculate  $[H_2A]$ ,  $[HA^-]$ ,  $[A^{2-}]$

$$[H^+] = \sqrt{K_{a1}[H_2A] + 2K_{a2}[HA^-] + K_w}$$