

Standard Addition Calculation and Error Analysis.

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You are interested in determining the concentration of an unknown solution C by fluorescence using the method of standard addition. Let's assume that you've made five solutions $C + n\Delta$ where $n=0-4$, and measure five fluorescence values, $F_0 - F_4$. This leads to five (x,y) data points:

$(C, F_0), (C + \Delta, F_1), (C + 2\Delta, F_2), (C + 3\Delta, F_3), (C + 4\Delta, F_4)$.

If we graph the following five (x,y) data points:

$(0, F_0), (\Delta, F_1), (2\Delta, F_2), (3\Delta, F_3), (4\Delta, F_4)$.

We will get a straight line that can be fit with the linear equation

$$y = mx + b$$

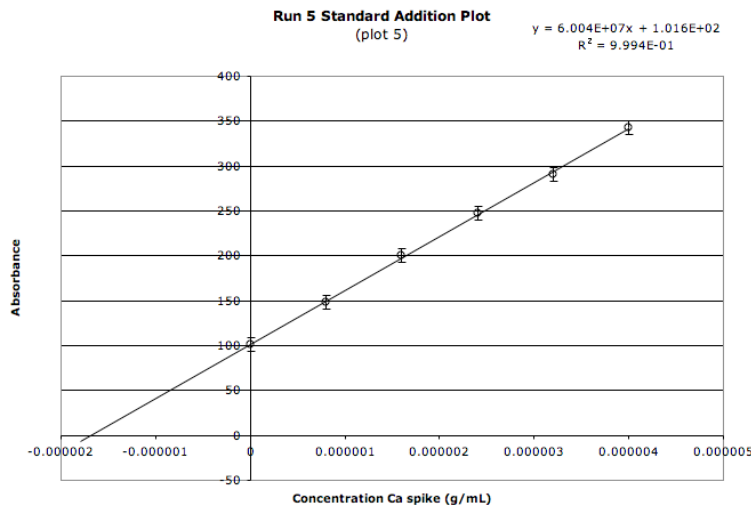
This line is the same line as a standard calibration curve, but shifted to the left by an amount equal to $-C$. To get the value of C, we set $y=0$ and calculate the value for the x intercept $x_0 = x$ at $y=0$:

$$x_0 = -b/m = -C$$

therefore:

$$C = b/m \text{ in units of } \Delta.$$

Here's a picture from Wikipedia:



Error analysis for the method of standard addition:

$$C = b/m$$

$$95\% \text{ C.L.} = \pm t_{N-2} s_c$$

We need to calculate s_c . Here's the result of the statistical derivation:

$$s_c = \frac{s_r}{m} \sqrt{\frac{1}{N} + \frac{(\bar{y})^2}{m^2 S_{xx}}}$$

This equation is similar to the equation we use for the linear calibration curve from Skoog with $y_c = 0$ and no $1/C$ term.