

Chem 249 Problem Set 2

R. Corn
Winter 2018

Three Phase Fresnel Calculation

1. Now that you've learned how to do it for two phases, create an Igor Pro file to calculate the Reflectivity for p-polarized and s-polarized light (R_p and R_s) as a function of incident angle from normal incidence (0 degrees) to grazing incidence (90 degrees) in 0.1 degree increments for the following THREE phase system where the index of refraction n_1 is real, and the indices of refraction of n_2 and n_3 can be complex:

i) $n_1 := 1.51$ (silica)

ii) $n_2 := 0.18 + 3.40i$ (gold)

iii) $n_3 := 1.00 + 0i$ (air)

iv) $\lambda = 633$ nm

v) $h :=$ initial value 45.0, vary h in a box by increments of 1 nm.

See the Hansen Paper for detailed equations. For Igor Pro, a text file of the refined History emailed to me is the most useful, along with an initial print out.

Frequency Domain Fluorescence Measurements

2. Frequency domain fluorescence spectroscopy (fdfs) is an alternative method for obtaining fluorescence lifetimes. In these measurement, two parameters: a phase shift angle (ϕ) and demodulation factor (m), are measured. What is the mathematical relationship between these measured parameters and the fluorescence lifetime (τ)? How is τ extracted from the fdfs data?

Classical Simple Harmonic Oscillator and LaPlace Transforms

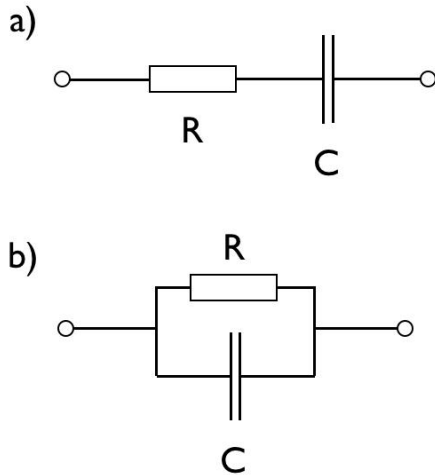
3. Consider the equation of motion for a damped harmonic oscillator:

$$m \frac{d^2 x}{dt^2} + 2m\Gamma \frac{dx}{dt} + m\omega^2 x = 0$$

with the initial conditions $x(0) = X_0$ and $x'(0) = V_0$. Use Laplace transforms to find $x(t)$ for the two cases where $\omega \gg \Gamma$ and $\omega = \Gamma$. Make plots in Igor of a couple of sample trajectories for these two cases.

Frequency Analysis: Nyquist and Bode Plots

4. Generate a Nyquist Impedance Plot and Bode Impedance plots (both magnitude and phase) for an angular frequency range of $10^{-2} \text{ rad s}^{-1}$ to 10^8 rad s^{-1} for these two RC circuits:



Where $R = 1000 \text{ ohms}$ and $C = 2.0 \text{ } \mu\text{F}$.

Complex Frequency Dependent Susceptibility: Optical Absorption Spectrum

5. Consider the classical equation of motion for an electron in a damped harmonic well:

$$m \frac{d^2 x}{dt^2} + 2m\Gamma \frac{dx}{dt} + m\omega_0^2 x = F(t)$$

where $F(t)$ is an externally applied Force. If $F(t) = qE(t) = -eE_0 \sin(\omega t)$, then the frequency dependent Polarization $P(\omega) = Ne x(\omega) = \chi(\omega) E(\omega)$ where N is the number of oscillators/volume, and $\chi(\omega)$ is called the frequency dependent electric susceptibility and has the form:

$$\chi(\omega) = \frac{S\omega_0^2}{\omega_0^2 - \omega^2 + i\omega\Gamma}$$

a) Please generate a plot of $\text{Im}\chi$ versus ω (a kind of Bode plot) for three cases where $S = 0.1$, $\omega_0 = 1000$, and $\Gamma = 10, 50, 100$. Measure the FWHM (full width at half max) for the resonant peak. How does it scale with Γ ?

b) Please generate a Nyquist plot ($\text{Im}\chi$ vs $\text{Re}\chi$) for the case $S = 0.1$, $\omega_0 = 1000$, and $\Gamma = 50$.

6. Using the general form for the general form for the electric susceptibility where $S = 0.1$, $\omega_0 = 1000$, and $\Gamma = 20$, please plot the real and imaginary parts of n , the complex index of refraction ($n = n_r + in_i$), versus omega. Recall that $n^2 = \epsilon_r = 1 + \chi$.